

H. Kuang · T. Richardson · S. Carson  
P. Wilcox · B. Bongarten

## Genetic analysis of inbreeding depression in plus tree 850.55 of *Pinus radiata* D. Don. I. Genetic map with distorted markers

Received: 20 April 1998 / Accepted: 13 July 1998

**Abstract** A genetic map of *Pinus radiata* plus tree 850.55 was constructed using megagametophytes of S<sub>1</sub> seeds. The map contained 19 linkage groups, with 168 RAPD and four microsatellite markers. The total map length was 1116.7 cM (Kosambi's function) and was estimated to cover 56% of the genome. Of the 172 markers, 59 (34%) were distorted from the expected 1:1 ratio in megagametophytes ( $P < 0.05$ ). We show that if the distortion is caused by a single viability gene or by sampling error, the estimate of recombination frequency in megagametophytes of selfed seeds would not be affected.

**Key words** Genetic linkage map · Segregation distortion · Megagametophyte · *Pinus radiata*

### Introduction

Radiata pine (*Pinus radiata* D. Don) is one of the more economically important forest tree species in the world, and particularly so in the southern hemisphere where breeding programs have been ongoing for almost 50 years (Balocchi 1997). These programs provide the majority of seed that is used to establish commercial plantations, usually by outcrossing trees of high breeding value.

Radiata pine, like most other conifers, displays inbreeding depression upon selfing, manifested as

reduced growth rate and seed set (reviewed by Williams and Savolainen 1996). In several tree species, segregation distortion of genetic markers has been found in progeny arising from inbreeding (Fowler 1964, 1965; Cheliak 1987; Hedrick and Muona 1990).

Reasons for segregation distortion in plants are not well understood but are thought to be related to factors such as chromosome loss (Kasha and Kao 1970), genetic isolating mechanisms (Zamir and Tadmor 1986), or viability genes (Hedrick and Muona 1990; Beavis and Grant 1991; Lin et al. 1992; Liedl and Anderson 1993; Bradshaw and Stettler 1994; Cheng et al. 1996; Xu et al. 1997). With respect to viability genes, selection may be at either the gametic level (Lin et al. 1992; Liedl and Anderson 1993; Yanagihara et al. 1995; Cheng et al. 1996; Xu et al. 1997) or the zygotic level (Hedrick and Muona 1990; Bradshaw and Stettler 1994). Non-biological factors such as scoring errors (Deve xy et al. 1994; Plomion et al. 1995) or sampling errors (Plomion et al. 1995; Echt and Nelson 1996) may also result in segregation distortion.

The availability of DNA marker systems has facilitated the development of moderate-dense linkage maps, therefore enhancing the power to detect segregation distortion. There have been numerous reports of segregation distortion from linkage experiments in plants, including forest trees (e.g., Helentjaris et al. 1986; McCouch et al. 1988; Nelson et al. 1993; Pillen et al. 1993; Bradshaw and Stettler 1994; Cheng et al. 1996; Xu et al. 1997).

In conifers, the use of the haploid megagametophyte of conifer seeds provides an efficient approach for constructing genetic maps of individual trees (Tulsieram et al. 1992; Nelson et al. 1993, 1994; Binelli and Bucci 1994; Plomion et al. 1995; Echt and Nelson 1997) and for detecting segregation distortion in the maternal parent. This mapping strategy is analogous to that for backcrosses with the linkage phase unknown (Nelson et al. 1993). However, the effect of distortion due to viability genes and sampling error on linkage analysis using megagametophytes has not yet been determined.

Communicated by P. M. A. Tigerstedt

H. Kuang · B. Bongarten (✉)  
Daniel B. Warnell School of Forest Resources, University of  
Georgia, Athens, Georgia, 30602-2152. USA

T. Richardson · S. Carson · P. Wilcox  
New Zealand Forest Research Institute Ltd, Private Bag 3020,  
Rotorua, NZ

In backcross populations, the classic estimate of recombination frequency between two markers is equal to the proportion of recombinants, which is identical to the maximum likelihood estimate (MLE). If a single viability gene (zygotic selection) is linked with the two markers, the estimate of recombination frequency is the same as when there is no viability disturbance (Bailey 1961). This result has not been extended to the use of conifer megagametophytes.

In this paper, we demonstrate that, under standard assumptions, the conventional maximum likelihood estimate of recombination is unbiased when genotypic data is obtained from megagametophytes, even when segregation distortion is present. Furthermore, we describe a linkage map of a high-value radiata pine tree, 850.055, that was constructed from megagametophyte genotypes of seed produced by artificial self pollination. Here, deviations from expected Mendelian ratios were frequently found.

## Materials and methods

### Plant materials and DNA extraction

Three hundred and seventy-eight selfed seeds of plus tree 850.55 were germinated singly in containers. Of the sown seeds 87 failed to germinate, leaving a total of 291 seeds that germinated successfully. Of these 291 seedlings 76 died within 1 month after germination; the remaining 215 seedlings survived for more than 1 year. Megagametophytes were collected from germinated seeds and stored at  $-20^{\circ}\text{C}$  until DNA extraction. Genomic DNA from megagametophytes of the 215 surviving individuals and 76 dead individuals was extracted using a Fast Prep FP 120 machine (Savant) and the Bio 101 Kit H. Of the 215 DNA samples from megagametophytes of surviving seedlings, 198 were chosen for map construction based on the quality of the DNA.

### Polymerase chain reaction (PCR) and random amplified polymorphic DNAs (RAPDs)

RAPD PCR was performed as previously described (Richardson et al. 1995), using 2.5 mM  $\text{MgCl}_2$ , 10 mM TRIS-HCl (pH 8.3), 50 mM KCl, 0.4 mM primer (Operon or UBC primers), 15 ng genomic DNA, 0.8 unit of *Taq* DNA polymerase, 0.2 mM of each of dNTPs, and deionized water (up to 25  $\mu\text{l}$ ) with a 50  $\mu\text{l}$  oil overlay. The PCR thermal cycle consisted of: 1 cycle of  $94^{\circ}\text{C}$  for 3 min /  $37^{\circ}\text{C}$  for 1 min /  $72^{\circ}\text{C}$  for 2 min, followed by 39 cycles of  $94^{\circ}\text{C}$  /  $37^{\circ}\text{C}$  /  $72^{\circ}\text{C}$  (1 min each), then 1 cycle at  $72^{\circ}\text{C}$  for 8 min. PCR was conducted in 96-well polycarbonate plates in a Techne PHC-3 thermal cycler. PCR products were separated by electrophoresis through a 1.5% agarose gel in  $1 \times$  TBE buffer. Gels were stained in 0.25 mg/ml ethidium bromide for 1 h, de-stained for 0.5 h, then photographed under UV light.

One hundred and twenty-five RAPD primers with segregating markers in plus tree 850.55 were initially selected (unpublished data). These primers were tested on DNA from needles and 6 megagametophytes of plus tree 850.55 to ensure that the expected bands were present and segregated. A total of 198 polymorphic markers were detected by 94 primers.

The names of the RAPD markers denote the supplier (U = UBC; otherwise, Operon) and primer name, followed by the size of the PCR fragment. The last letter in the marker name indicates the

marker quality, classified as A, B or C, according to band intensity and background of the null allele, with A being best and C worst. The case of marker names shows their linkage phase. For example, ai05800a is a good marker, with a band fragment size of 800 bp, amplified by Operon primer AI05; U327600B is a marker of medium quality, with a PCR fragment size of 600 bp, amplified by primer UBC327; the null allele of ai05800a and band allele of U327600B are in coupling phase.

Four previously published microsatellite markers were also utilized (Fisher et al. 1996; Smith and Devey 1994), giving a total of 202 markers.

The DNA of 198 megagametophytes of surviving seedlings was screened with all 202 markers. Segregation distortion, as measured by departure from the expected 1 : 1 ratio, was tested with chi-square analysis for each marker.

### Linkage analysis

Because the mapping strategy using megagametophytes of conifers is identical to that for backcrosses with phase unknown, the data file was modified so that both coupling and repulsion phases could be recognized (Nelson et al. 1993). A linkage map was constructed using MAPMAKER (Lander et al. 1987) version 3.0. Markers were assigned to linkage groups with  $\text{LOD} > 5$  and  $\theta < 0.25$ . The markers in each group were ordered using the "order" command, with interval support  $\text{LOD} > 3$  and error detection on (base threshold  $\text{LOD} > 1$ , net error threshold  $\text{LOD} > 5$ ). The resulting linkage order was checked using "ripple" command ( $\text{LOD}$  threshold = 3). Unsupported markers were listed at the side of their linkage group (Plomion et al. 1995). Map distance was calculated using Kosambi's function.

### Effects of viability genes on linkage analysis

Suppose a viability gene L is linked with two markers A and B, alleles A/B/L and a/b/l are in coupling phase, and the viabilities of the diploid genotype LL, lL and ll are 1,  $1 - hs$  and  $1 - s$ , respectively, where s is the selection coefficient and h is the degree of dominance. After selection, the expected genotype frequencies of megagametophytes of selfed seeds can be inferred. The effects of degree of dominance (h) and selection coefficient (s) on the estimation of recombination frequency are indicated by the combined frequencies of recombinants (aB and Ab) (see Appendix). It is shown that neither s nor h affect recombination rates, and thus do not affect the linkage analysis.

To demonstrate that viability genes had no effect on linkage analysis, we constructed and compared different maps using (1) megagametophytes of surviving seedlings, (2) megagametophytes of dead seedlings, and (3) both. Contingency chi-square tests were performed to test the difference of interval recombination frequencies among maps.

### Analysis of co-migrating RAPD bands

Five bands which showed strong segregation distortion were examined to determine if the distortion could be caused by co-migrating bands. To do so, the PCR fragments were purified from RAPD agarose gel using DNA Purification Kits (Bio-Rad, Calif., USA) following the manufacturer's instructions. The purified fragments were re-amplified with the original RAPD primer under the same conditions as those described above, digested with *Mse*, then separated in a 2% agarose gel. If the sum of lengths for the digested products was greater than the length of the DNA in the original band, co-migrating bands were indicated.

## Results

### Linkage analysis

All 198 RAPD and four microsatellite markers were initially included for linkage analysis using MAP-MAKER (Lander et al. 1987), ignoring segregation distortion. Markers were assigned to 19 linkage groups with  $\theta < 0.25$  and  $\text{LOD} > 5$ . Six markers unlinked with any group were also detected, and these were not included in the map. The markers in each group were ordered using the “order” command, with interval support  $\text{LOD} > 3$  and error detection on (base threshold  $\text{LOD} > 1$ , net error threshold  $\text{LOD} > 5$ ). The resulting linkage order was checked using command “ripple” ( $\text{LOD}$  threshold = 3). Un-supported markers were listed at the side of their linkage group. The resulting map, shown in Fig. 1, contained 168 RAPD and four microsatellite markers, covering 1116.7 cM. The longest linkage group, Group 1, was 136.4 cM. It had 28 markers and hosted a locus with a lethal allele responsible for seedling death (Kuang et al. 1998). Using the method of Chakravarti et al. (1991) we calculated the total genome length of radiata pine to be 1979 cM (Kosambi's), with a 95% confidence interval of 1830–2148 cM. Therefore, the map covered approximately 56% of the genome.

The causes of segregation distortion and their effects on linkage analysis

Of the 172 markers ultimately mapped, 59 were distorted from a 1:1 ratio in the megagametophytes of selfed seeds ( $P < 0.05$ ). Of these, 49 were clustered in 10 discrete regions; 10 were scattered in the linkage groups (Fig. 1).

### Scoring errors

The un-supported markers, which were listed at the side of linkage groups, were likely to have many scoring errors. If an un-supported marker was distorted but its linked marker in the framework was not, the segregation distortion was most likely caused by scoring problems. Five of the un-supported markers were chosen to test for co-migrating polymorphic bands. Two markers, U256700B (138 megagametophytes with band allele versus 47 with null allele) and U322850B (122 with band allele versus 44 with null allele), were found to be composed of several different fragments (co-migrating polymorphic bands).

### Sampling error

Of the 172 markers 9 were expected to be distorted ( $P < 0.05$ ) by chance (type-I errors, ignoring linkage).

Which distorted markers were due to sampling error in this experiment is not clear. If the distortion is due to sampling error, the estimation of recombination frequency between markers is unbiased (not shown). When the markers are distorted at a very high level (e.g.,  $P < 0.001$ ), it is unlikely that their distortion is by chance.

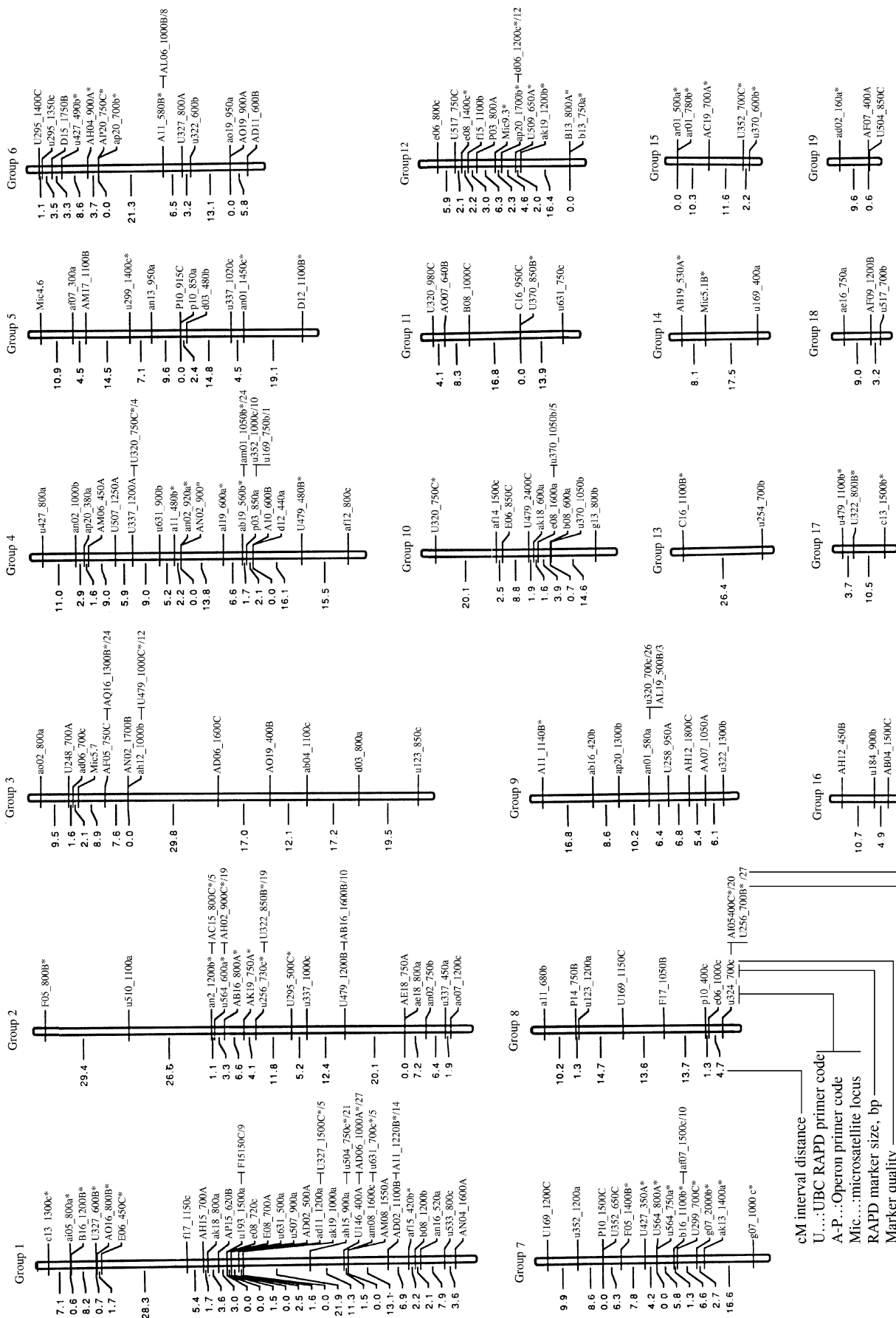
Faint bands, when unable to be scored explicitly, were scored as “data missing”. If most of the unscored individuals belong to one genotype, false distortion might occur. However, this type of distorted marker should not show more double recombinants than expected, and its flanking markers should show a normal segregation ratio. The ten distorted markers that did not occur in clusters might be caused by this type of sampling error. Like distortion by chance, this type of distortion also does not affect linkage analysis (not shown).

### Viability genes

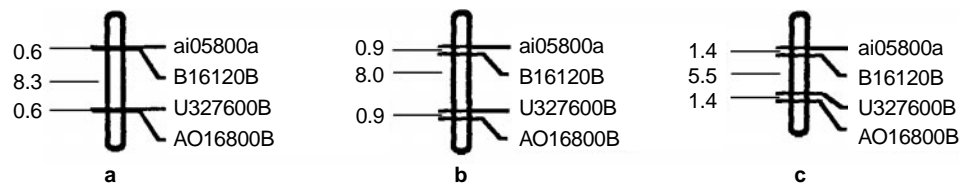
Segregation distortion of DNA markers may also have a biological basis. Gametic or zygotic selection will cause skewed segregation of viability genes, and the markers that are highly linked with them. There is no evidence for gametic selection in conifers, and gametic selection should not cause the reduced seed set, germination, and survival following germination which are evident in this population. In this study, ten discrete distorted regions were identified. Their distortion might be caused by viability genes acting in zygotic selection. However, we could not exclude the possibility that some of them were caused by sampling errors.

Distortion caused by zygotic selection due to a single viability gene does not affect the estimate of recombination frequency between markers in megagametophytes of selfed seeds. This is demonstrated in the appendix. There, it is shown that for a viability gene  $L$  present between markers  $A$  and  $B$  ( $A-L-B$ ), the classical estimate of recombination frequency between the markers is  $r_1 + r_2 - 2r_1r_2$ , which is the same as when there is no viability disturbance. The estimate of the recombination frequency is independent of selection coefficient or degree of dominance of the viability gene. This is also true when the viability gene is located on either side of the two markers (not shown).

An example that a single viability gene does not affect linkage analysis in megagametophytes of selfed seeds is shown in Fig. 2. A lethal allele responsible for seedling death was discovered previously (Kuang et al. 1998). After selection under this gene, the surviving seedlings lacked homozygotes of the lethal allele, whereas all dead seedlings were homozygotes for the lethal allele. The linkage map constructed using the megagametophytes of surviving seedlings is shown in Fig. 2a, and the linkage map using megagametophytes of dead seedlings is shown in Fig. 2c. Markers in both



cM interval distance  
 U...: UBC RAPD primer code  
 A-P...: Operon primer code  
 Mic...: microsatellite locus  
 RAPD marker size, bp  
 Marker quality  
 Segregation distortion  
 cM(K) distance from framework locus



**Fig. 2a–c** Segregation distortion due to a single viability gene does not affect linkage analysis. Linkage group was constructed using megagametophytes of surviving seedlings (a), all seedlings (b), and dead seedlings (c)

data sets were highly distorted ( $P < 0.0001$ ), but in favor of different alleles. When these two data sets were combined, markers showed normal segregation, and the resulting linkage group is shown in Fig. 2b. As shown in Fig 2, these maps are consistent in marker order. Contingency chi-square test indicates that the interval recombination frequencies are not significantly different among these maps.

## Discussion

A genetic map with 19 linkage groups (pines have 12 chromosomes) was constructed for radiata pine plus tree 850.55 using megagametophytes of selfed seeds. This map has 168 RAPD and four microsatellite markers, covering 1116.7 cM. This map is consistent with a previous map which shared 38 markers, except that the linkage order between markers an 01580a and U258100 A in linkage group 9 was reversed. Using the method of Chakravarti et al. (1991), we estimated the total genome length of radiata pine to be 1979 cM (K), with a 95% confidence interval of 1830–2148 cM. This is a typical estimate for pine species (Echt and Nelson 1997).

Of the 172 markers 59 were distorted from the expected 1:1 segregation ratio ( $P < 0.05$ ). Fifty-one of them were clustered in ten discrete regions; 8 were scattered elsewhere. Segregation distortion might result from sampling or scoring errors or from lethal/sub-lethal genes. Gametic selection may also cause segregation distortion. However, gametic selection should not result in inbreeding depression. There is no evidence for self-incompatibility in conifers prior to fertilization (Hagman and Mikkola 1963).

We showed that the estimation of recombination frequency was consistent for markers which were distorted in megagametophytes of  $S_1$  seeds due to sampling error or a single viability gene. It has been shown that the estimation of recombination frequency is

biased in backcross and  $F_2$  mapping populations if there are two viability genes controlling the segregation of markers (Lorieux et al. 1995a,b). That is also true for megagametophytes of  $S_1$  seeds. However, the effects of two (or more) linked deleterious genes on linkage analysis in megagametophytes of  $S_1$  seeds are beyond the scope of this paper. We assumed that a maximum of one viability gene was responsible for each discrete distorted region in the construction of the map presented here. In practice, it is difficult to distinguish whether one or several highly linked viability genes are responsible for the segregation distortion of markers in one region. If two linked deleterious alleles are in coupling phase, their effects on segregation are similar to those of a single viability gene. If they are in repulsion phase, their effects on segregation are similar to those of a single overdominant gene (pseudo-overdominance). Overdominant and pseudo-overdominant viability genes will change the segregation ratio of diploid genotypes, but they may not disturb the segregation ratio in megagametophytes. Like a dominant viability gene, a single overdominant viability gene does not affect the estimation of recombination frequency between nearby markers (data not shown).

Scoring errors might be so high for bad markers (e.g., some RAPDs) that distortion appears. Heteroduplex and co-migrating polymorphic bands (Plomion et al. 1995), if not recognized, might have a strongly skewed ratio. For example, two independent segregating bands of similar size will be undistinguishable in the gel, resulting in a ratio of band allele to null allele in megagametophytes of  $S_1$  seeds of 3:1 rather than 1:1.

Though conifer megagametophytes are an ideal material for genetic mapping, they have a few limitations. First, only PCR-based markers can be used because of the small amount of DNA in megagametophytes. Secondly, megagametophyte genotypes may not be efficient for genetic analysis because the traits of interest are mainly for diploid tissues. Megagametophyte genotypes can only show the maternal contribution, and only the additive effects of quantitative trait loci can be determined (Plomion et al. 1996). Genotyping both megagametophyte and diploid tissues with dominant markers cannot solve this problem completely, but it may provide further information for genetic analysis (Kuang et al. 1998).

**Acknowledgements** We thank Drs. Wayne Parrott and Scott Merkle for reviewing this manuscript, the Gene Mapping and Fingerprinting group of NZFRI for helping H.K.'s laboratory work, John Lee for planting the selfed seedlings and collecting tissue samples. We hereby declare that the experiments comply with the current laws of New Zealand and USA.

**Fig. 1** Genetic linkage map of plus tree 850.55 of *P. radiata*. Asterisks denote that segregation of marker is skewed from a 1:1 ratio

## References

- Bailey NTJ (1961) Mathematical theory of genetic linkage. Oxford University Press, Amen House, London
- Beavis WD, Grant D (1991) A linkage map based on information from four F<sub>2</sub> populations of maize (*Zea mays* L.). *Theor Appl Genet* 82: 636–644
- Binelli G, Bucci G (1994) A genetic linkage map of *Picea abies* Karst., based on RAPD markers, as a tool in population genetics. *Theor Appl Genet* 88: 283–288
- Bradshaw HD, Stettler RF (1994) Molecular genetics of growth and development in *Populus*. II. Segregation distortion due to genetics load. *Theor Appl Genet* 89: 551–558
- Chakravarti A, Lasher LK, Reefer JE (1991) A maximum-likelihood method for estimating genome length using genetic linkage data. *Genetics* 128: 175–182
- Cheng R, Saito A, Takano Y, Ukai Y (1996) Estimation of the position and effect of a lethal factor locus on a molecular marker linkage map. *Theor Appl Genet* 93: 494–502
- Devey ME, Fiddler TA, Liu BH, Knapp SJ (1994) An RFLP linkage map for loblolly pine based on a three-generation outbred pedigree. *Theor Appl Genet* 88: 273–278
- Devey ME, Bell JC, Smith DN, Neale DB (1996) A genetic linkage map for *Pinus radiata* based on RFLP, RAPD, and microsatellite markers. *Theor Appl Genet* 92: 673–679
- Echt CS, Nelson CD (1997) Linkage mapping and genome length in eastern white pine (*Pinus strobus* L.). *Theor Appl Genet* 94: 1031–1037
- Fisher PJ, Gardner RC, Richardson TE (1996) Single locus microsatellites isolated using 5' anchored PCR. *Nucleic Acids Res* 24: 4369–4371
- Hagman M, Mikkola L (1963) Observations on cross-, self- and interspecific pollinations in *Pinus peuce* Griseb. *Silv Genet* 12: 73–79
- Hedrick PW, Muona O (1990) Linkage of viability genes to marker loci in selfing organisms. *Heredity* 64: 67–72
- Helentjaris T, Slocum M, Wright S, Schaefer A, Nienhuis J (1986) Construction of genetic linkage maps in maize and tomato using restriction fragment length polymorphisms. *Theor Appl Genet* 72: 761–769
- Kasha KJ, Kao KN (1970) High frequency haploid production in barley (*Hordeum vulgare* L.). *Nature* 225: 874–876
- Kuang H, Richardson TE, Carson SD, Bongarten BC (1998) An allele responsible for seedling death in *Pinus radiata* D. Don. *Theor Appl Genet* 96: 640–644
- Lander ES, Green P, Abrahamson J, Baarlow A, Daly MJ (1987) MAPMAKER: an interactive computer package for constructing primary genetic linkage maps of experimental and natural populations. *Genomics* 1: 174–181
- Liedl B, Anderson NO (1993) Reproductive barriers: identification of an intraspecific integrated linkage map of pepper using molecular markers and doubled-haploid progenies. *Genome* 38: 112–121
- Lin SY, Ikehashi S, Yanagihara S, Kawashima A (1992) Segregation distortion via male gametes in hybrids between *Indica* and *Japonica* or wide-compatibility varieties of rice (*Oryza sativa* L.). *Theor Appl Genet* 84: 814–818
- Lorieux M, Goffinet B, Perrier X, Gonzalez de Leon D, Lanaud C (1995a) Maximum-likelihood models for mapping genetic markers showing segregation distortion. 1. Backcross populations. *Theor Appl Genet* 90: 73–80
- Lorieux M, Perrier X, Goffinet B, Lanaud C, Gonzalez de Leon D (1995b) Maximum-likelihood models for mapping genetic markers showing segregation distortion. 2. F<sub>2</sub> populations. *Theor Appl Genet* 90: 81–89
- Lyttle TW (1991) Segregation disorders. *Annu Rev Genet* 25: 511–557
- McCouch SR, Kochert G, Yu ZH, Wang ZY, Khush GS, Coffman WR, Tanksley SD (1988) Molecular mapping of rice chromosomes. *Theor Appl Genet* 76: 815–829
- Nelson CD, Nance WL, Doudrick RL (1993) A partial genetic linkage map of slash pine (*Pinus elliottii* Engelm. var 'elliottii') based on random amplified polymorphic DNAs. *Theor Appl Genet* 87: 145–151
- Nelson CD, Kubisiak TL, Stine M, Nance WL (1994) A genetic linkage map of longleaf pine (*Pinus palustris* Mill.) based on random amplified polymorphic DNAs. *J Hered* 85: 433–439
- Pillen K, Steinrucken G, Herrmann RG, Jung C (1993) An extended linkage map of Sugar Beet (*Beta vulgaris* L.) including nine putative lethal genes and the restorer gene X. *Plant Breed* 111: 265–272
- Plomion C, O'Malley DM, Durel C-E (1995) Genomic analysis in maritime pine (*Pinus pinaster*). Comparison of two RAPD maps using selfed and open-pollinated seeds of the same individual. *Theor Appl Genet* 90: 1028–1034
- Plomion C, Durel C-E, O'Malley DM (1996) Genetic dissection of height in maritime pine seedlings raised under accelerated growth conditions. *Theor Appl Genet* 93: 849–858
- Richardson T, Cato S, Ramser J, Kahl G, Weising K (1995) Hybridization of microsatellites to RAPD: a new source of polymorphic markers. *Nucleic Acids Res* 23: 3798–3799
- Smith DN, Devey ME (1994) Occurrence and inheritance of microsatellites in *Pinus radiata*. *Genome* 37: 977–983
- Tulsieram LK, Glaubitz JC, Kiss G, Carlson J (1992) Single tree genetic linkage mapping using haploid DNA from megagametophytes. *Bio/Technology* 10: 686–690
- Xu Y, Zhu L, Xizo J, Huang N, McCouch SR (1997) Chromosomal regions associated with segregation distortion of molecular markers in F<sub>2</sub>, backcross, doubled haploid, and recombinant inbred populations in rice (*Oryza sativa* L.). *Mol Gen Genet* 253: 535–545
- Yanagihara S, McCouch SR, Ishikawa K, Ogi Y, Maruyama K, Ikehashi H (1995) Molecular analysis of the inheritance of the S-5 locus, conferring wide compatibility in *Indica/Japonica* hybrids of rice (*O. Sativa* L.). *Theor Appl Genet* 90: 182–188
- Zamir D, Tadmor Y (1986) Unequal segregation of nuclear genes in plants. *Bot Gaz* 147: 355–358

## Appendix

Megagametophyte genotype frequency after selection of gene  $L^a$

♂	♀ gamete genotype	AB		Ab	
		ALB (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) <sup>b</sup>	A/B r <sub>1</sub> r <sub>2</sub>	ALb (1 - r <sub>1</sub> )r <sub>2</sub>	A/b r <sub>1</sub> (1 - r <sub>2</sub> )
ALB	(1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) <sup>b</sup>	(1 - r <sub>1</sub> ) <sup>2</sup> (1 - r <sub>2</sub> ) <sup>2</sup> <sup>c</sup> 1 <sup>d</sup>	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1 - hs	r <sub>2</sub> (1 - r <sub>1</sub> ) <sup>2</sup> (1 - r <sub>2</sub> ) 1	r <sub>1</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) <sup>2</sup> 1 - hs
A/B	r <sub>1</sub> r <sub>2</sub>	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1 - hs	r <sub>1</sub> <sup>2</sup> r <sub>2</sub> <sup>2</sup> 1 - s	r <sub>1</sub> r <sub>2</sub> <sup>2</sup> (1 - r <sub>1</sub> ) 1 - hs	r <sub>1</sub> <sup>2</sup> r <sub>2</sub> (1 - r <sub>2</sub> ) 1 - s
ALb	(1 - r <sub>1</sub> )r <sub>2</sub>	r <sub>2</sub> (1 - r <sub>1</sub> ) <sup>2</sup> (1 - r <sub>2</sub> ) 1	r <sub>1</sub> r <sub>2</sub> <sup>2</sup> (1 - r <sub>1</sub> ) 1 - hs	r <sub>2</sub> <sup>2</sup> (1 - r <sub>1</sub> ) <sup>2</sup> 1	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1 - hs
Alb	r <sub>1</sub> (1 - r <sub>2</sub> )	r <sub>1</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) <sup>2</sup> 1 - hs	r <sub>1</sub> <sup>2</sup> r <sub>2</sub> (1 - r <sub>2</sub> ) 1 - s	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1 - hs	r <sub>1</sub> <sup>2</sup> (1 - r <sub>2</sub> ) <sup>2</sup> 1 - s
aLB	r <sub>1</sub> (1 - r <sub>2</sub> )	r <sub>1</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) <sup>2</sup> 1	r <sub>1</sub> <sup>2</sup> r <sub>2</sub> (1 - r <sub>2</sub> ) 1 - hs	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1	r <sub>1</sub> <sup>2</sup> (1 - r <sub>2</sub> ) <sup>2</sup> 1 - hs
a/B	(1 - r <sub>1</sub> )r <sub>2</sub>	r <sub>2</sub> (1 - r <sub>1</sub> ) <sup>2</sup> (1 - r <sub>2</sub> ) 1 - hs	r <sub>1</sub> r <sub>2</sub> <sup>2</sup> (1 - r <sub>1</sub> ) 1 - s	r <sub>2</sub> <sup>2</sup> (1 - r <sub>1</sub> ) <sup>2</sup> 1 - hs	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1 - s
alb	(1 - r <sub>1</sub> )(1 - r <sub>2</sub> )	(1 - r <sub>1</sub> ) <sup>2</sup> (1 - r <sub>2</sub> ) <sup>2</sup> 1 - hs	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1 - s	r <sub>2</sub> (1 - r <sub>1</sub> ) <sup>2</sup> (1 - r <sub>2</sub> ) 1 - hs	r <sub>1</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) <sup>2</sup> 1 - s
aLb	r <sub>1</sub> r <sub>2</sub>	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1	r <sub>1</sub> <sup>2</sup> r <sub>2</sub> <sup>2</sup> 1 - hs	r <sub>1</sub> r <sub>2</sub> <sup>2</sup> (1 - r <sub>1</sub> ) 1	r <sub>1</sub> <sup>2</sup> r <sub>2</sub> (1 - r <sub>2</sub> ) 1 - hs
∑ (after selection)		[(1 - r <sub>1</sub> )(1 - r <sub>2</sub> )(2 - hs) + r <sub>1</sub> r <sub>2</sub> (2 - hs - s)]		[(1 - r <sub>1</sub> )r <sub>2</sub> (2 - hs) + r <sub>1</sub> (1 - r <sub>2</sub> )(2 - hs - s)]	
Female gamete genotype frequency		[(1 - r <sub>1</sub> )(1 - r <sub>2</sub> )(2 - hs) + r <sub>1</sub> r <sub>2</sub> (2 - hs - s)] 4 - 2hs - s		[(1 - r <sub>1</sub> )r <sub>2</sub> (2 - hs) + r <sub>1</sub> (1 - r <sub>2</sub> )(2 - hs - s)] 4 - 2hs - s	
Recombination frequency		r <sub>1</sub> + r <sub>2</sub> - 2r <sub>1</sub> r <sub>2</sub>			

♂	♀ gamete genotype	aB		ab	
		ALB r <sub>1</sub> (1 - r <sub>2</sub> )	a/B (1 - r <sub>1</sub> )r <sub>2</sub>	alb (1 - r <sub>1</sub> )(1 - r <sub>2</sub> )	aLb r <sub>1</sub> r <sub>2</sub>
ALB	(1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) <sup>b</sup>	r <sub>1</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) <sup>2</sup> 1	r <sub>2</sub> (1 - r <sub>1</sub> ) <sup>2</sup> (1 - r <sub>2</sub> ) 1 - hs	(1 - r <sub>1</sub> ) <sup>2</sup> (1 - r <sub>2</sub> ) <sup>2</sup> 1 - hs	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1
A/B	r <sub>1</sub> r <sub>2</sub>	r <sub>1</sub> <sup>2</sup> r <sub>2</sub> (1 - r <sub>2</sub> ) 1 - hs	r <sub>1</sub> r <sub>2</sub> <sup>2</sup> (1 - r <sub>1</sub> ) 1 - s	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1 - s	r <sub>1</sub> <sup>2</sup> r <sub>2</sub> <sup>2</sup> 1 - hs
ALb	(1 - r <sub>1</sub> )r <sub>2</sub>	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1	r <sub>2</sub> <sup>2</sup> (1 - r <sub>1</sub> ) <sup>2</sup> 1 - hs	r <sub>2</sub> (1 - r <sub>1</sub> ) <sup>2</sup> (1 - r <sub>2</sub> ) 1 - hs	r <sub>1</sub> r <sub>2</sub> <sup>2</sup> (1 - r <sub>1</sub> ) 1
Alb	r <sub>1</sub> (1 - r <sub>2</sub> )	r <sub>1</sub> <sup>2</sup> (1 - r <sub>2</sub> ) <sup>2</sup> 1 - hs	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1 - s	r <sub>1</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) <sup>2</sup> 1 - s	r <sub>1</sub> <sup>2</sup> r <sub>2</sub> (1 - r <sub>2</sub> ) 1 - hs
aLB	r <sub>1</sub> (1 - r <sub>2</sub> )	r <sub>1</sub> <sup>2</sup> (1 - r <sub>2</sub> ) <sup>2</sup> 1	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1 - hs	r <sub>1</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) <sup>2</sup> 1 - hs	r <sub>1</sub> <sup>2</sup> r <sub>2</sub> (1 - r <sub>2</sub> ) 1
a/B	(1 - r <sub>1</sub> )r <sub>2</sub>	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1 - hs	r <sub>2</sub> <sup>2</sup> (1 - r <sub>1</sub> ) <sup>2</sup> 1 - s	r <sub>2</sub> (1 - r <sub>1</sub> ) <sup>2</sup> (1 - r <sub>2</sub> ) 1 - s	r <sub>1</sub> r <sub>2</sub> <sup>2</sup> (1 - r <sub>1</sub> ) 1 - hs
alb	(1 - r <sub>1</sub> )(1 - r <sub>2</sub> )	r <sub>1</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) <sup>2</sup> 1 - hs	r <sub>2</sub> (1 - r <sub>1</sub> ) <sup>2</sup> (1 - r <sub>2</sub> ) 1 - s	(1 - r <sub>1</sub> ) <sup>2</sup> (1 - r <sub>2</sub> ) <sup>2</sup> 1 - s	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1 - hs
aLb	r <sub>1</sub> r <sub>2</sub>	r <sub>1</sub> <sup>2</sup> r <sub>2</sub> (1 - r <sub>2</sub> ) 1	r <sub>1</sub> r <sub>2</sub> <sup>2</sup> (1 - r <sub>1</sub> ) 1 - hs	r <sub>1</sub> r <sub>2</sub> (1 - r <sub>1</sub> )(1 - r <sub>2</sub> ) 1 - hs	r <sub>1</sub> <sup>2</sup> r <sub>2</sub> <sup>2</sup> 1
∑ (after selection)		[r <sub>1</sub> (1 - r <sub>2</sub> )(2 - hs) + (1 - r <sub>1</sub> )r <sub>2</sub> (2 - hs - s)]		[r <sub>1</sub> r <sub>2</sub> (2 - hs) + (1 - r <sub>1</sub> )(1 - r <sub>2</sub> )(2 - hs - s)]	
Female gamete genotype frequency		[r <sub>1</sub> (1 - r <sub>2</sub> )(2 - hs) + (1 - r <sub>1</sub> )r <sub>2</sub> (2 - hs - s)] 4 - 2hs - s		[r <sub>1</sub> r <sub>2</sub> (2 - hs) + (1 - r <sub>1</sub> )(1 - r <sub>2</sub> )(2 - hs - s)] 4 - 2hs - s	
Recombination frequency		r <sub>1</sub> + r <sub>2</sub> - 2r <sub>1</sub> r <sub>2</sub>			

<sup>a</sup> A and B are two markers, and  $L$  is the viability gene. Linkage order: A-r<sub>1</sub>-L-r<sub>2</sub>-B, where r<sub>1</sub> and r<sub>2</sub> are recombination rates

<sup>b</sup> Gamete genotype frequency. 1/2 is omitted

<sup>c</sup> Diploid genotype frequency. 1/4 is omitted

<sup>d</sup> Viability of the corresponding diploid genotype